

Eskişehir Osmangazi University - Electrical Engineering Department
Advanced Calculus
1st Midterm Examination - Summer 2012

!!! For each problem put the answer next to it !!!

1. [40 pts.] Evaluate the following (express the results in cartesian form):

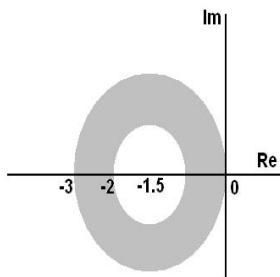
$$\overline{(2+i)^3} \text{ Ans. } 2 - 11i$$

$$\operatorname{Log}e^{2+i} \text{ Ans. } 2 + i$$

$$\sin(1+3i) \text{ Ans. } 8.47 + 5.41i$$

$$4^i \text{ Ans. } (0.184 + 0.983i)e^{2\pi n}, \quad n = 0, \pm 1, \dots$$

2. [20 pts.] Sketch $1 < |2z + 3| < 3$



3. [20 pts.] If exists, find derivative $\frac{df}{dz}$ of $f(z) = x^2 - y^2 + x + i2xy + iy + 3$
Ans. $2z + 1$
4. [20 pts.] Evaluate $\int_{\gamma} z dz$ where $\gamma : 2e^{i\theta}, \quad 0 \leq \theta \leq 2\pi$ **Ans.** 0
A. Karamancioğlu