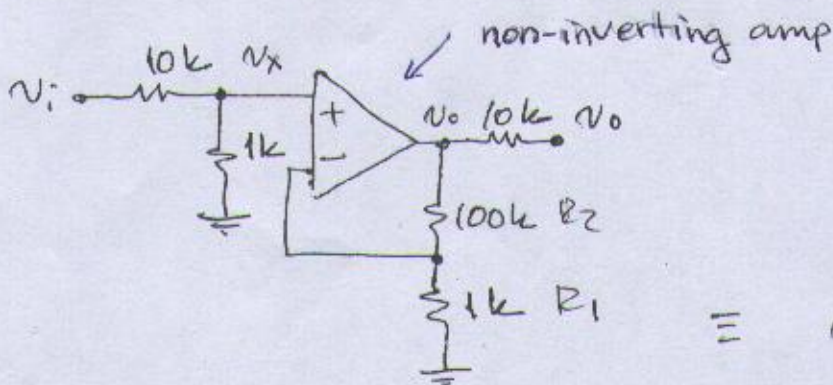


ID number: ERKAYA Name: SOLUTIONS Signature: _____

- 1) Find the input resistance, output resistance and open circuit voltage gain of the amplifier given below.

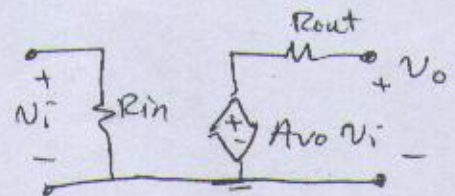
q:44



$$R_{in} = 11k$$

$$R_{out} = 10k$$

$$A_{vo} = V_o/V_i = 9.18$$



$$\text{gain } \frac{V_o}{V_x} = 1 + \frac{R_2}{R_1} = 101$$

$$\frac{V_x}{V_i} = \frac{1}{10+1} = \frac{1}{11}$$

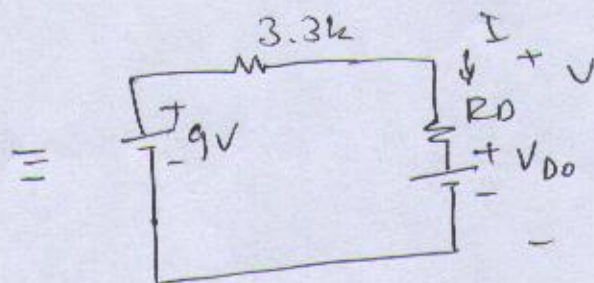
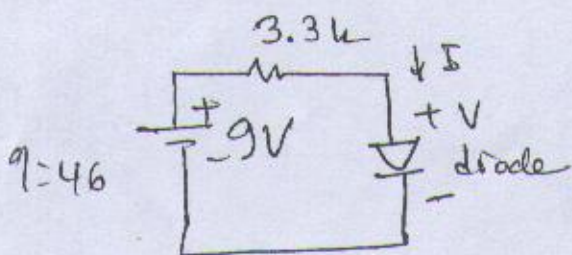
$$\frac{V_o}{V_i} = 101 \times \frac{1}{11} = \frac{101}{11} = 9.18$$

$$R_{in} = 10k + 1k = 11k$$

$$R_o = 10k \text{ by inspection}$$

q:46

- 2) A diode has 1 mA at 0.60 V and 11 mA at 0.72 V. Find a DC model for the diode if it is used in the circuit below:



$$V = V_{D0} + I R_D$$

$$V_1 = V_{D0} + I_1 R_D$$

$$V_2 = V_{D0} + I_2 R_D$$

$$V_2 - V_1 = (I_2 - I_1) R_D$$

$$R_D = \frac{V_2 - V_1}{I_2 - I_1} = \frac{0.72 - 0.60}{11 - 1 \text{ mA}} = \frac{0.12 \text{ V}}{10 \text{ mA}} = 0.012 \text{ k}\Omega = \underline{\underline{12 \Omega}}$$

$$V_{D0} = V_1 - I_1 R_D = 0.60 - 0.012 \times 1 = \underline{\underline{0.588 \text{ V}}}$$

$$V_{D0} = 0.588 \text{ V}$$

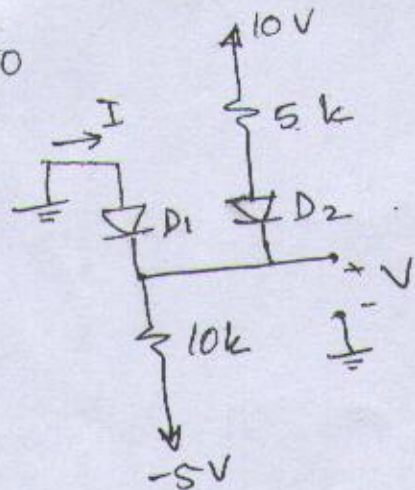
$$R_D = 12 \Omega$$

q=50

3) Find I and V in the circuit below (diodes are ideal).

$I = \underline{0}$, $V = \underline{5V}$

Q:50



Assume $D1 = \text{OFF}$
 $D2 = \text{ON}$

$$I_{D2} = \frac{10 - (-5)}{5 + 10} = 1 \text{ mA}$$

$$V = 10 - 5 \times 1 = 5 \text{ V.}$$

The voltage on $D1$ is $0 - 5 = -5 \text{ V} < 0$

→ $D1$ is OFF.

Hence $I = 0$
 $V = 5 \text{ V}$

Q:52

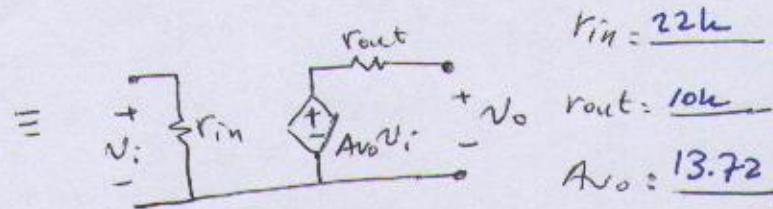
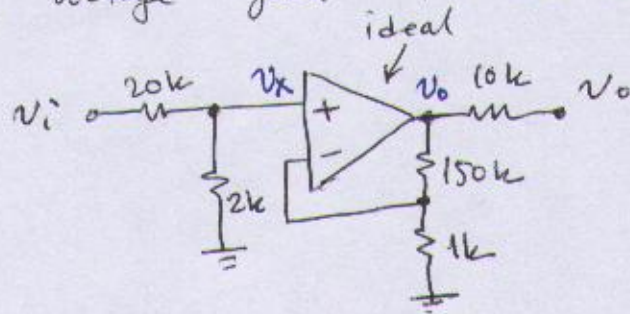
10.11.2005

Electronics I - Midterm 1 - 60 minutes

ID number: ERKAYA Name: SOLUTIONS Signature: _____

1) Find the input resistance, output resistance and open-circuit voltage gain for the amplifier given below:

20pt



$$r_{in} = 20k + 2k = 22k$$

$$r_{out} = 10k + 0k = 10k$$

↑
ideal opamp

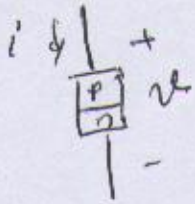
no load $\rightarrow$ output of opamp = V_o

$$\frac{V_o}{V_x} = \frac{1 + 150}{1} = 151$$

$$\frac{V_x}{V_i} = \frac{2}{20 + 2} = \frac{1}{11}$$

$$A_{v0} = \frac{V_o}{V_i} = \frac{V_o}{V_x} \cdot \frac{V_x}{V_i} = 151 \times \frac{1}{11} = 13.72$$

- 2) A pn-junction diode has the following voltage and current values. a) Find a non-linear model for the diode. b) Find a piece-wise linear model for the diode.



v	i
0.60 V	0.1 mA
0.74 V	11.1 mA

$$V_T = 0.025 \text{ V}$$

a) ideality factor $\eta = 1.189$
reverse sat. current $I_S = 1.71 \times 10^{-10} \text{ A}$

a)

$$i = I_S (e^{v/\eta V_T} - 1) \cong I_S e^{v/\eta V_T}$$

$$0.1 = I_S e^{0.6/\eta \cdot 0.025}$$

$$11.1 = I_S e^{0.74/\eta \cdot 0.025}$$

dividing side by side

$$III = e^{(0.74 - 0.60)/\eta \cdot 0.025}$$

$$\ln(III) = \frac{0.14}{\eta \cdot 0.025} \rightarrow \eta = \frac{0.14}{0.025 \ln III} = 1.189$$

$$11.1 = I_S e^{0.74/1.189 \times 0.025} = 6.47 \times 10^{-10} I_S$$

$$I_S = \frac{11.1}{6.47 \times 10^{-10}} = 1.71 \times 10^{-10} \text{ A}$$

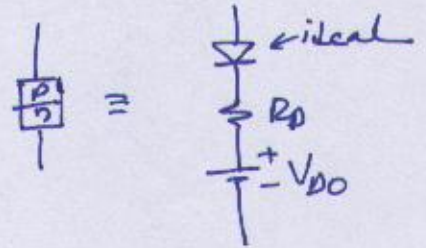
b)

$$R_D = \frac{\Delta V}{\Delta i} = \frac{0.74 - 0.60}{11.1 - 0.1} = 0.0127 \text{ k}\Omega = 12.7 \Omega$$

$$0.6 = V_{D0} + 0.1 \times 0.0127$$

$$V_{D0} = 0.6 - 0.00127 = 0.5987 \text{ V}$$

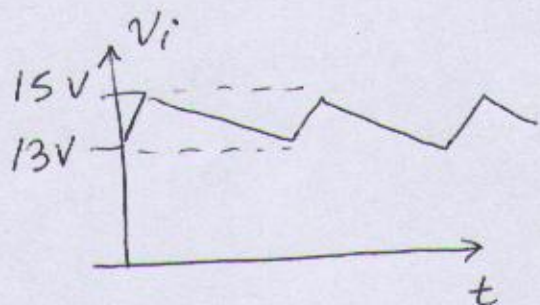
b)



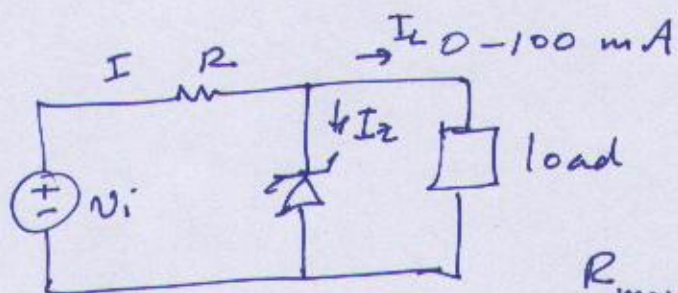
$$R_D = 12.7 \Omega$$

$$V_{D0} = 0.5987 \text{ V}$$

- 3) Design a shunt regulator to obtain 9V output voltage. The load requires 0-100 mA current. The input voltage is as shown below:



Specify the power rating of the components you use in your design



Zener diode $V_{ZE} = 9V$
the same as the output voltage

$$R_{max} = \frac{V_{imin} - V_o}{I_{Lmax} + I_{Zmin}}$$

assume $I_{Zmin} = 1mA$

$$R_{max} = \frac{13 - 9}{101} = 0.0396 k = 39.6 \Omega$$

Power rating for zener diode:

Max current in zener is when $V_i \rightarrow V_{imax} = 15V$
 $I_L \rightarrow I_{Lmin} = 0$

$$I_z = I_{max} - I_{Lmin} = \frac{15 - 9}{39.6} - 0 = 0.1515 A$$

$$P_{Zmax} = 9 \times 0.1515 = \underline{\underline{1.36 W}}$$

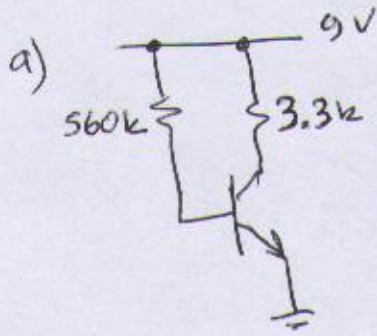
Power rating for R :

$$I_{max}^2 R = (0.1515)^2 \times 39.6 = \underline{\underline{0.91 W}}$$

R: 39.6 W, 0.91 W

Zener: 9V, 1.36 W

4) Find the operating points for the BJTs in the ccts
30pt given below: $V_{BE} = 0.7V$, $\beta = 100$



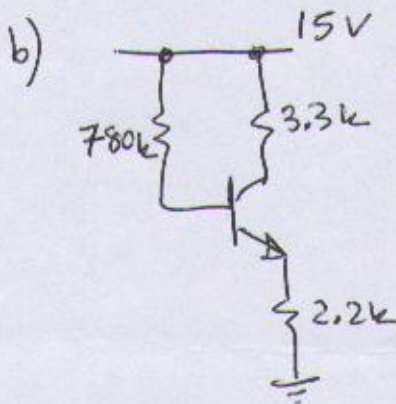
$$I_C = 1.48 \text{ mA}$$

$$V_{CE} = 4.10 \text{ V}$$

$$I_B = \frac{9 - 0.7}{560k} = 0.0148 \text{ mA}$$

$$I_C = 100 I_B = 1.48 \text{ mA}$$

$$V_{CE} = 9 - 3.3 \times 1.48 = 4.10 \text{ V}$$



$$I_C = 1.427 \text{ mA}$$

$$V_{CE} = 7.12 \text{ V}$$

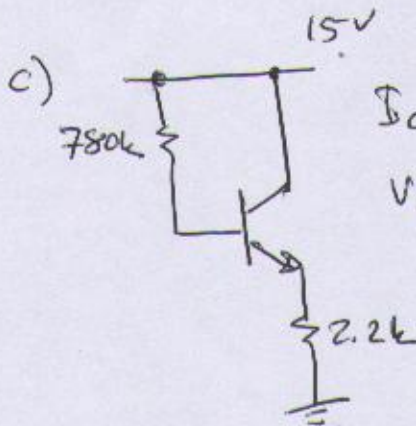
$$(I_B + I_C) \times 2.2 + 0.7 + I_B 780 = 15$$

$$I_C = \beta I_B = 100 I_B$$

$$I_B = \frac{15 - 0.7}{2.2 \times 101 + 780} = 0.01427 \text{ mA}$$

$$I_C = \beta I_B = 1.427 \text{ mA}$$

$$V_{CE} = 15 - 2.2 \times \frac{101}{100} \times 1.427 - 3.3 \times 1.427 = 7.12 \text{ V}$$



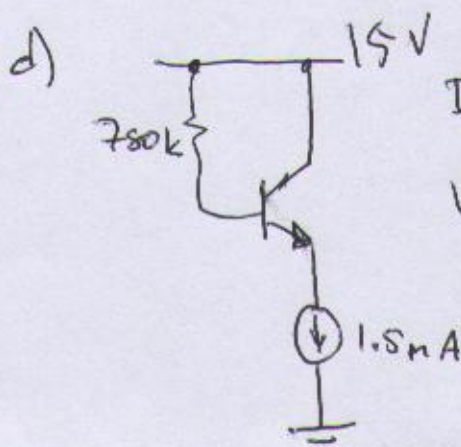
$$I_C = 1.427$$

$$V_{CE} = 11.87 \text{ V}$$

I_B is the same as in (b)

$$I_C = 1.427 \text{ mA}$$

$$V_{CE} = 15 - 2.2 \times \frac{101}{100} \times 1.427 = 11.87 \text{ V}$$



$$I_C = 1.485 \text{ mA}$$

$$V_{CE} = 12.28 \text{ V}$$

$$I_C = \frac{100}{101} I_E = \frac{1.5}{1.01} = 1.485 \text{ mA}$$

$$V_{CE} = 15 - V_E, \quad I_B = 0.01485 \text{ mA}$$

$$V_E = V_B - V_{BE} = 15 - 780 I_B - 0.7 = 2.717 \text{ V}$$

$$V_{CE} = 15 - 2.717 = 12.28 \text{ V}$$

I have neither given nor received any unauthorized help with this exam, nor do I have any reason to believe that anybody else has.

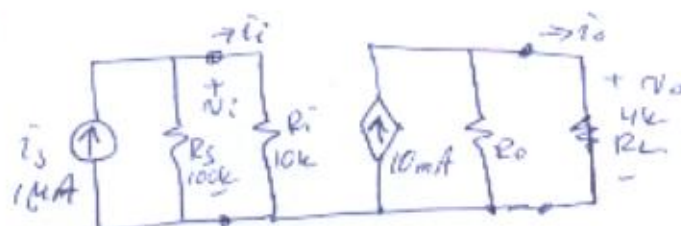
ID number: _____ Name: SOLUTIONS Signature: _____

1. An amplifier with an input resistance of $10\text{ k}\Omega$, when driven by a current source of $1\text{ }\mu\text{A}$ and a source resistance of $100\text{ k}\Omega$, has a short-circuit output current of 10 mA and an open-circuit output voltage of 10 V . When driving a $4\text{-k}\Omega$ load, what are the values of the voltage gain, current gain, and power gain expressed as ratios and in dB?

$$A_v = \frac{880}{1} \quad (58.89\text{ dB})$$

$$A_i = \frac{2198}{1} \quad (66.84\text{ dB})$$

$$A_p = \frac{1.934 \times 10^6}{1} \quad (62.86\text{ dB})$$



$$10\text{ mA} \times R_o = 10\text{ V}$$

$$R_o = \frac{10\text{ V}}{10\text{ mA}} = 1\text{ k}\Omega$$

$$V_o = 10\text{ mA} \times 1\text{ k}\Omega \parallel 4\text{ k}\Omega = 10 \times 0.8 = 8\text{ V}$$

$$V_i = 0.001\text{ mA} \times (100\text{ k}\Omega \parallel 10\text{ k}\Omega) = 0.001 \times 9.09 = 0.0091\text{ V}$$

$$A_v = \frac{V_o}{V_i} = \frac{8}{0.0091} = 880 \rightarrow 20 \log(880) = 58.89\text{ dB}$$

$$i_i = \frac{0.0091}{10\text{ k}} = 0.00091\text{ mA} = 0.91\text{ }\mu\text{A}$$

$$i_o = \frac{V_o}{R_L} = \frac{8}{4\text{ k}} = 2\text{ mA}$$

$$A_i = \frac{2\text{ mA}}{0.91\text{ }\mu\text{A}} = 2198 \rightarrow 20 \log(2197.8) = 66.84\text{ dB}$$

$$A_p = \frac{V_o \times i_o}{V_i \times i_i} = A_v \cdot A_i = 880 \times 2198 = 1.934 \times 10^6 \rightarrow$$

$$10 \log(1.934 \times 10^6) = 62.86\text{ dB}$$

2. In designing with op amps one has to check the limitations on the voltage and frequency ranges of operation of the closed-loop amplifier, imposed by the op amp finite bandwidth (f_c), slew rate (SR), and output saturation (V_{max}). This problem illustrates the point by considering the use of an op amp with $f_c = 2.5 \text{ MHz}$, $\text{SR} = 1.2 \text{ V}/\mu\text{s}$, and $V_{max} = 10 \text{ V}$ in the design of a noninverting amplifier with a nominal gain of 10. Assume a sine-wave input with peak amplitude V_i .

- (a) If $V_i = 0.5 \text{ V}$, what is the maximum frequency before the output distorts?
 (b) If $f = 20 \text{ kHz}$, what is the maximum value of V_i before the output distorts?
 (c) If $V_i = 50 \text{ mV}$, what is the useful frequency range of operation?
 (d) If $f = 5 \text{ kHz}$, what is the useful input voltage range?

a) $V_i = 0.5 \text{ V}$, $V_o = 0.5 \times 10 = 5 \text{ V}$

$$f_{\max} = \frac{\text{SR}}{2\pi V_o} = \frac{1.2 \times 10^6}{2\pi \times 5} = 38.197 \text{ kHz}$$

a) $f_{\max} = 38.197 \text{ kHz}$

b) $V_{i\max} = 0.955 \text{ V}$

c) $f_{\text{range}} = 0 - 250 \text{ kHz}$

d) $V_i \text{ range} = 0 - 1 \text{ V}$

b) $f = 20 \text{ kHz}$, $V_o \leq \frac{\text{SR}}{2\pi f} = \frac{1.2 \times 10^6}{2\pi \times 20 \times 10^3} = 9.55 \text{ V}$
 $V_i = \frac{V_o}{10} = 0.955 \text{ V}$

c) $V_i = 50 \text{ mV}$, $V_o = 10 \times 50 \text{ mV} = 500 \text{ mV} = 0.5 \text{ V}$

$$f_{\max} = \frac{\text{SR}}{2\pi V_o} = \frac{1.2 \times 10^6}{2\pi \times 0.5} = 381.9 \text{ kHz}$$

There maybe another restriction/limitation $\rightarrow$ gain-bandwidth product

$$f_{\max} \times \text{gain} = f_c \rightarrow f_{\max} = \frac{f_c}{\text{gain}} = \frac{2.5 \times 10^6}{10} = 250 \text{ kHz}$$

Since 250 kHz is smaller than 381.9 kHz , the freq. range (bandwidth) is limited by 250 kHz

d) $f = 5 \text{ kHz}$, slew rate limitation: $V_o \leq \frac{\text{SR}}{2\pi f} = \frac{1.2 \times 10^6}{2\pi \times 5 \times 10^3} = 38.19 \text{ V}$

However, the supply voltages limit the output voltage to 10 V . (given) Hence, the input voltage is limited by $\frac{10 \text{ V}}{10} = 1 \text{ V}$. Useful range $0 - 1 \text{ V}$.

3. Assuming that the diodes in the circuits of Fig. P3 are ideal, utilize Thévenin's theorem to simplify the circuits and thus find the values of the labeled currents and voltages.

$$\begin{aligned} I_a &= \underline{0.225 \text{ mA}} \\ V_a &= \underline{4.5 \text{ V}} \\ I_b &= \underline{0} \\ V_b &= \underline{-2 \text{ V}} \end{aligned}$$

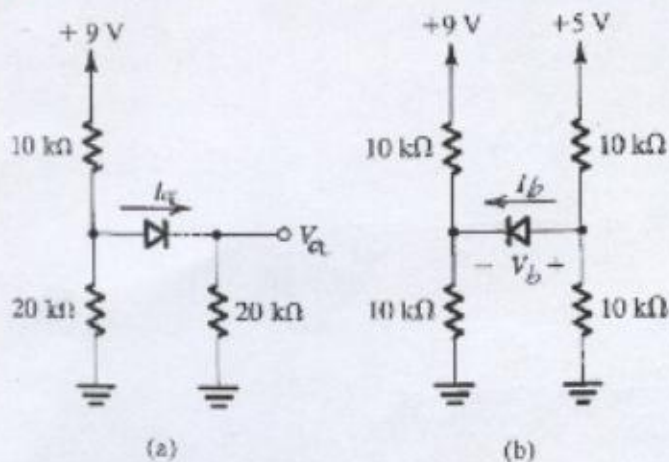
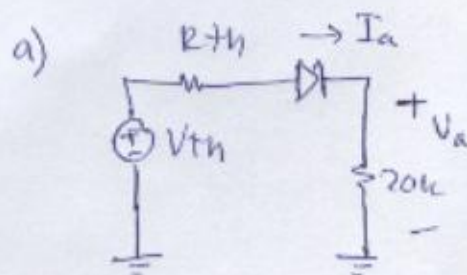


FIGURE P3

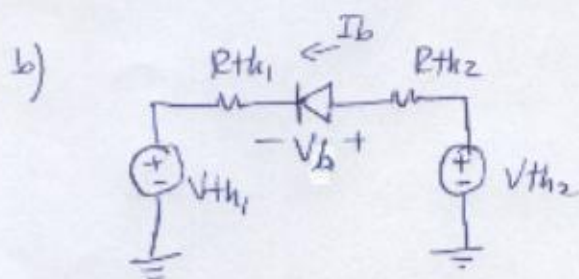


$$R_{th} = 10k \parallel 20k = 6.66k$$

$$V_{th} = 9 \times \frac{20}{10+20} = 6 \text{ V}$$

$$I_a = \frac{V_{th}}{(20 + 6.66)k} = \frac{6}{26.66} = 0.225 \text{ mA}$$

$$V_a = I_a \times 20k = 4.5 \text{ V}$$



$$R_{th1} = 10k \parallel 10k = 5k\Omega$$

$$V_{th1} = 9 \times \frac{10}{10+10} = 4.5 \text{ V}$$

$$R_{th2} = 10k \parallel 10k = 5k\Omega$$

$$V_{th2} = 5 \times \frac{10}{10+10} = 2.5 \text{ V}$$

Since $V_{th1} > V_{th2}$, the diode will be reverse biased.

$$V_{th1} + V_b = V_{th2}$$

$$V_b = V_{th2} - V_{th1} = 2.5 - 4.5 = -2 \text{ V.}$$

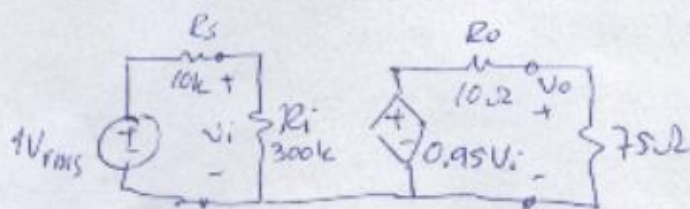
$$I_b = 0 \text{ for reverse bias}$$

ID number: ERKAYA Name: SOLUTIONS Signature: _____

- 1) A common collector BJT amplifier draws 2.5 mA from a 9V power supply. The amplifier has $300\text{ k}\Omega$ input resistance and $10\text{ }\Omega$ output resistance. If it is connected to a signal source whose open circuit voltage is 1 V rms and whose short circuit current is 0.1 mA rms , and if it has a load of $75\text{ }\Omega$, what would be its voltage gain, current gain, power gain, and efficiency?

→ open circuit voltage gain 0.95

$$P_{DC} = 2.5 \times 9 = 22.5\text{ mW}$$



$$P_s = \frac{1\text{ V}}{0.1\text{ mA}} = 10\text{ k}\Omega$$

$$\frac{V_o}{V_i} = \frac{0.84}{1}$$

$$\frac{i_o}{i_i} = \frac{3360}{1}$$

$$\frac{P_o}{P_i} = \frac{2820}{1}$$

$$\eta = \frac{0.391}{1}$$

$$\text{open circuit - voltage gain} = 0.95$$

$$\frac{V_o}{V_i} = 0.95 \times \frac{75}{10+75} = 0.84$$

$$\frac{i_o}{i_i} = \frac{V_o/75}{V_i/300} = \frac{V_o}{V_i} \times \frac{300}{75} = 0.84 \times 4000 = 3.36\text{ k} = 3360$$

$$\frac{P_o}{P_i} = \frac{V_o \cdot i_o}{V_i \cdot i_i} = 4 \left(\frac{V_o}{V_i} \right)^2 = 2820$$

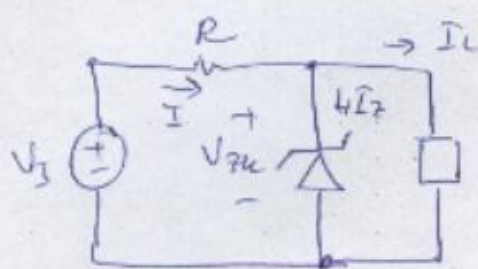
$$P_o = \frac{V_o^2}{75\text{ }\Omega}$$

$$V_i = \frac{300}{310}\text{ V rms}, V_o = 0.95 \times \frac{75}{85} \times \frac{300}{310} = 0.811\text{ V rms}$$

$$P_o = \frac{(0.811)^2}{75\text{ }\Omega} = 0.0088\text{ W} = 8.8\text{ mW}$$

$$\eta = \frac{P_o}{P_{DC}} = \frac{8.8}{22.5} = 0.391$$

2) Designing a shunt regulator with a Zener diode to provide 0-60 mA to a load at constant voltage of 9.1 V. The input source has the peak voltage 13.5 V and a peak-to-peak ripple of 1.5 V. Specify the component values and power ratings that you use in your design.



$$V_{ZK} = 9.1 \text{ V}$$

$$V_{Imin} = 13.5 - 1.5 = 12 \text{ V}$$

$$V_{Imax} = 13.5 \text{ V}$$

$$\text{Let } I_{Zmin} = 1 \text{ mA}$$

$$R = \frac{V_{Imin} - V_o}{I_{Lmax} + I_{Zmin}} = \frac{12 - 9.1}{61 \text{ mA}}$$

$$R = \frac{2.9}{61 \text{ mA}} = 47.5 \Omega$$

$$P_{Rmax} = R I_{max}^2$$

$$I_{max} = \frac{V_{Imax} - V_o}{R} = \frac{13.5 - 9.1}{47.5} = 0.0926 \text{ A} = 92.6 \text{ mA}$$

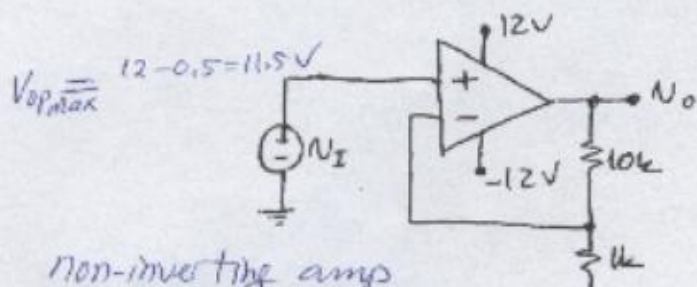
$$P_{Rmax} = 47.5 \times (0.0926)^2 = 0.407 \text{ W}$$

$$P_{Zmax} = 9.1 \times I_{max} = 0.0926 \times 9.1 = 0.84 \text{ W}$$

$$R \text{ power rating} \geq 0.4 \text{ W} \rightarrow 0.5 \text{ W}$$

$$Z_{env} \text{ " " } \geq 0.84 \text{ W} \rightarrow 1 \text{ W}$$

3) In the amplifier below, the opamp has a gain-bandwidth product of 1800 kHz, slew rate of 0.8 V/ μ s.



Non-inverting amp

$$\text{gain} = 1 + \frac{10}{1} = 11$$

$$\text{Bandwidth} = \frac{1800 \text{ kHz}}{11} = 163.6 \text{ kHz}$$

The output voltage can approach the supply voltages no closer than 0.5V.

$$V_i = V_{IP} \sin \omega t, \text{ no distortion is desired}$$

a) If $V_{IP} = 0.6V$, what would be the max signal frequency?

b) If $f = 30 \text{ kHz}$, what would be the max V_{IP} ?

c) If $V_{IP} = 30 \text{ mV}$, what is the max signal frequency?

d) If $f = 3 \text{ kHz}$, what would be the max V_{IP} ?

$$\text{max } V_{IP} = \underline{\hspace{2cm}}$$

$$\text{max } f = \underline{\hspace{2cm}}$$

$$\text{max } V_{IP} = \underline{\hspace{2cm}}$$

$$\begin{aligned} \text{a) } 2\pi f V_{OP} &\leq SR \\ f &\leq \frac{SR}{2\pi V_{OP}} = \frac{0.8 \times 10^6}{2\pi \times 0.6 \times 11} = 19291 \text{ Hz} \end{aligned}$$

$$\text{b) } V_{OP} \leq \frac{SR}{2\pi f} = \frac{0.8 \times 10^6}{2\pi \times 30 \times 10^3} = 4.244 \text{ V}, \quad V_{IP_{\text{max}}} = \frac{4.244}{11} = 0.386 \text{ V}.$$

$$\begin{aligned} \text{c) } V_{IP} = 30 \text{ mV}, \quad V_{OP} = 330 \text{ mV} \quad f &\leq \frac{SR}{2\pi V_{OP}} = \frac{0.8 \times 10^6}{2\pi \times 0.33} = 385.8 \text{ kHz} \\ \text{since the bandwidth is } 163.6 \text{ kHz,} \\ \text{max freq. of the signal is } 163.6 \text{ kHz.} \end{aligned}$$

$$\text{d) } V_{OP} = \frac{SR}{2\pi f} = \frac{0.8 \times 10^6}{2 \times \pi \times 3000} = 42.4 \text{ V not possible}$$

$$V_{OP} \leq 12 - 0.5 = 11.5 \text{ V} \quad V_{IP} \leq 1.045 \text{ V}.$$