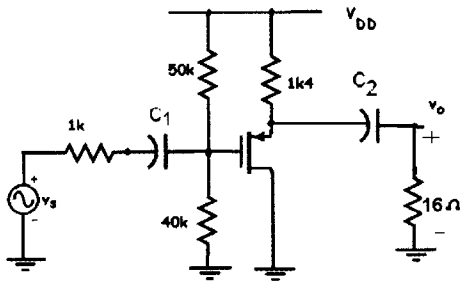


ID number: ERKAYH Name: SOLUTIONS Signature: _____

- 45 pts 1) Select C_1 and C_2 in a way that the low 3 dB cutoff frequency of the amplifier given below is 300 Hz. Assume $K=32 \text{ mA/V}^2$, $I_D = 2 \text{ mA}$.



$$g_m = 2\sqrt{KI_D} = 2\sqrt{32 \times 2} = 16 \text{ mA/V}$$

$$C_1 = \frac{6.85 \times 10^{-6} \text{ F}}{7 \times 10^{-6} \text{ F}}$$

$$\frac{1}{g_m} = \frac{1}{16} = 0.0625 \text{ k}\Omega$$

There are two poles f_1 and f_2 .

$$f_c \approx f_1 + f_2$$

$$\text{Set } f_2 = 299 \text{ Hz}$$

$$f_1 = 1 \text{ Hz}$$

$$f_1 = \frac{1}{2\pi C_1 R_{th1}}$$

$$f_2 = \frac{1}{2\pi C_2 R_{th2}}$$

no unique solution

$$R_{th1} = 1k + 50k \parallel 40k = 23.22k\Omega$$

$$R_{th2} = 16\Omega + \frac{1}{g_m} \parallel 1.4k \approx 76\Omega$$

$$C_1 = \frac{1}{2\pi f_1 R_{th1}} = \frac{1}{2\pi \times 1 \times 23220} = 6.85 \times 10^{-6} \text{ F}$$

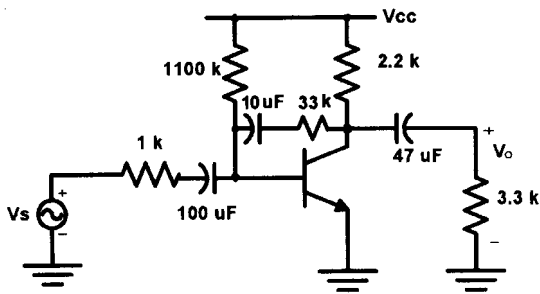
$$C_2 = \frac{1}{2\pi f_2 R_{th2}} = \frac{1}{2\pi \times 299 \times 76} = 7 \times 10^{-6} \text{ F}$$

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55 pts 2) Using Miller's theorem, find the high 3dB cutoff frequency of the amplifier given below.

Assume $\beta = 240$, $I_C = 1.50 \text{ mA}$, $C_\mu = 1.7 \text{ pF}$, $f_T = 450 \text{ MHz}$, $r_x = 0 \text{ ohms}$, $r_o = 120 \text{ k}$

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$$g_m = \frac{1.5}{0.025} = 60 \text{ mA/V}$$

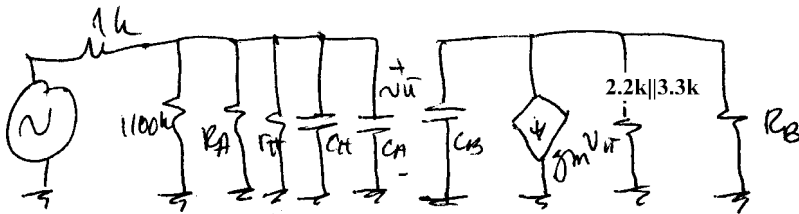
$$f_H \approx 3.8 \text{ MHz}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{240}{60} = 4 \text{ k}\Omega$$

$$C_\pi = \frac{g_m}{2\pi f_T} - C_\mu = \frac{60 \times 10^{-3}}{2\pi \times 450 \times 10^6} - 1.7 \times 10^{-12} = 19.52 \text{ pF}$$

Apply Miller's theorem on 33k and C_μ

$$|g_m R_{sh}| \gg 1 \rightarrow R_B \approx 33 \text{ k}\Omega$$



$$R_{sh} = 2.2 \text{ k}\Omega \parallel 3.3 \text{ k}\Omega \parallel 33 \text{ k}\Omega$$

$$\approx 1.27 \text{ k}\Omega$$

$$g_m R_{sh} = 60 \times 1.27 = 76.15$$

$$C_B \approx C_\mu = 1.7 \text{ pF}$$

$$R_A = \frac{33 \text{ k}}{1 + g_m R_{sh}} = \frac{33 \text{ k}}{77.15} = 0.427 \text{ k}$$

$$\omega_A = \frac{1}{R_{thA} (C_A + C_\pi)} =$$

$$R_{thA} = R_{sig} \parallel R_A \parallel 1100 \text{ k}\Omega \parallel 1 \text{ k}\Omega$$

$$= 4 \parallel 0.427 \parallel 1100 \parallel 1 \text{ k} = 0.278 \text{ k}$$

$$\omega_A = \frac{1}{0.278 \times (131.2 + 19.52) \times 10^{-12}} = 23.87 \text{ Mrad/s}$$

$$C_\pi = C_\mu (1 + g_m R_{sh}) = 1.7 \times 77.15 = 131.2 \text{ pF}$$

$$\omega_B = \frac{1}{C_B R_{sh}} = \frac{1}{1.7 \times 10^{-12} \times 1270} = 463 \times 10^6 \text{ rad/s}$$

$$\omega_B \gg \omega_A \quad \text{Hence} \quad \omega_H \approx \omega_A \rightarrow f_H = \frac{23.87 \times 10^6}{2\pi} = 3.799 \text{ MHz}$$

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