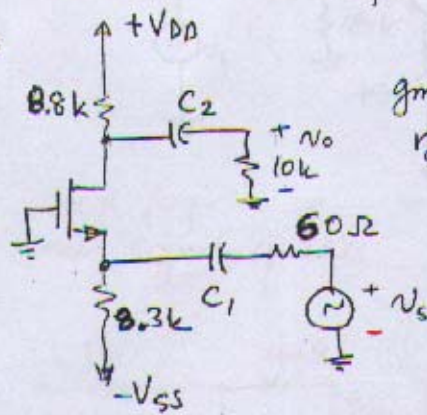


Adı soyadı: SOLUTIONS İmza: _____ Öğrenci No: _____

1) Select the values of C_1 and C_2 in the ckt below such that the 3-dB low cut-off frequency is 200 Hz or less.

40 pts



$$g_m = 12 \text{ mA/V} \quad C_{gs} = 1 \text{ pF}$$

$$r_{ds} \rightarrow \infty \quad C_{ds} = 1 \text{ pF}$$

$$C_{gd} = 1 \text{ pF}$$

$$C_1 = 5.63 \times 10^{-6} \text{ F}$$

$$C_2 = 8.46 \times 10^{-6} \text{ F}$$

There are two LF poles f_1 and f_2

Let $f_1 = 199 \text{ Hz}$, $f_2 = 1 \text{ kHz}$ so that

$$f_1 + f_2 = 200 \text{ Hz}$$

$$R_{th1} = 8.3 \text{ k} \parallel \frac{1}{g_m} + 60 \Omega$$

$$= (8.3 \text{ k} \parallel \frac{1}{12} \text{ k} + 0.060 \text{ k})^{\dagger} = 0.142 \text{ k}\Omega$$

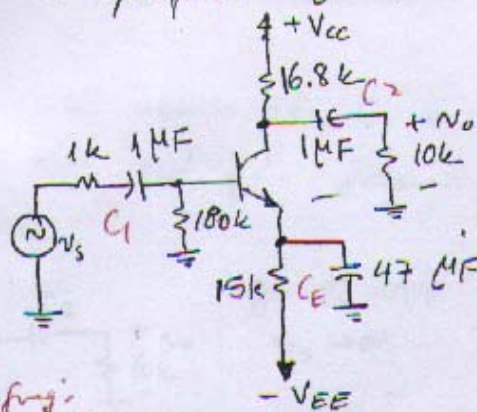
$$R_{th2} = 8.8 + 10 = 18.8 \text{ k}\Omega$$

$$C_1 = \frac{1}{2\pi f_1 R_{th1}} = \frac{1}{2\pi \times 199 \times 142} = 5.63 \times 10^{-6} \text{ F}$$

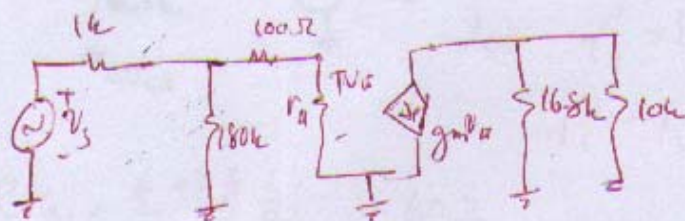
$$C_2 = \frac{1}{2\pi f_2 R_{th2}} = \frac{1}{2\pi \times 1 \times 18800} = 8.46 \times 10^{-6} \text{ F}$$

2) Using Miller's theorem, find the high and low cut-off frequencies of the amplifier given below.

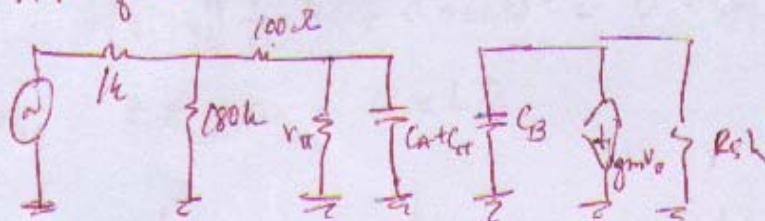
60 pts



mid freq.
Small signal eq. ckt.



HF eq. ckt



Two HF poles $\rightarrow$ $\omega_H = \frac{1}{(R_{thA} + C_{\pi})R_{thB}}$, $\omega_B = \frac{1}{C_B R_{thB}}$

$$R_{thA} = r_{\pi} \parallel (1k + 1 \parallel 180) = 6 \parallel 1.1 = 0.929 k\Omega$$

$$R_{thB} = R_{sh} = 6260 \Omega$$

$$\omega_A = \frac{1}{(15.4 + 157) \times 10^{-12} \times 0.929} = 6.24 \times 10^6 \text{ rad/s}$$

$$\omega_B = \frac{1}{0.5 \times 10^{-12} \times 6260} = 319 \times 10^6 \text{ rad/s}$$

$$\omega_H = \frac{1}{\frac{1}{\omega_A} + \frac{1}{\omega_B}} \approx \omega_A \text{ since } \omega_A \ll \omega_B$$

For Low freq $\rightarrow$ $R_{th1} = 1k + (180k \parallel 6k) \approx 7k$ (C_E - short)

$$R_{th2} = 16.8k + 10k = 26.8k \Omega$$

$$R_{thE} = 15k \parallel \frac{r_{\pi} + r_e + (180 \parallel 1)k}{\beta + 1} = 15 \parallel \frac{(6.1 + 1)k}{301} \approx 23.6 \Omega$$

$$\omega_L \approx \frac{1}{1 \times 10^6 + 70000} = 142.8 \text{ rad/s}$$

$$\omega_2 = \frac{1}{1 \times 10^6 \times 26800} = 37.3 \text{ rad/s}$$

$$\omega_{EE} = \frac{1}{47 \times 10^6 \times 23.6} = 901 \text{ rad/s}$$

$$\omega_1 \rightarrow \text{recalc. w/ CE open} \rightarrow \omega_1 = 5.52 \text{ rad/s}$$

$$\omega_L = 943 \text{ rad/s}$$

$$\omega_H = 6.24 \times 10^6 \text{ rad/s}$$

$$g_m = \frac{1.25}{0.025} = 50 \text{ mA/V}$$

$$r_{\pi} = \frac{300}{50} = 6 k\Omega$$

$$R_{sh} = 16.8k \parallel 10k = 6.26k$$

$$g_m R_{sh} = 313$$

$$C_{\pi} = \frac{g_m}{2\pi f_T} - C_{\mu} = \frac{50 \times 10^{-3}}{2\pi \times 500 \times 10^6} - 0.5 \times 10^{-12} = 15.4 \text{ pF}$$

$$C_{\pi} = 15.4 \times 10^{-12} - 0.5 \times 10^{-12} = 15.4 \text{ pF}$$

$$C_A = C_{\mu}(1 + g_m R_{sh}) = 157 \text{ pF}$$

$$C_B \approx C_{\mu} = 0.5 \text{ pF}$$

$$\omega_L \approx 37.3 + 5.52 = 42.8 \text{ rad/s}$$

This is a closed-book, closed-notes exam. Write your answer to the space provided below each question. If you need more space, use the back of the sheet and indicate the question number. Read the questions carefully. Do not use any time on any question more than what you allocate in the beginning of the exam. Good Luck!

I have neither given nor received unauthorized help with this work; nor do I have reason to believe that anybody else has.

Student ID: _____ Name: ERKAYA Signature: SOLUTIONS Grade: _____

1. (50 pts) Find the input resistance, output resistance and the voltage gain v_{out}/v_s for the amplifier given in Figure 1. ($g_m = 33 \text{ mA/V}$, $R_D = 5 \text{ k}\Omega$, $R_F = 250 \text{ k}\Omega$, $R_G = 1 \text{ M}\Omega$, $R_S = 5 \text{ k}\Omega$)

$$v_{out}/v_s = \underline{-38.22}$$

$$R_{in} = \underline{1.5 \text{ k}\Omega}$$

$$R_{out} = \underline{\hspace{2cm}}$$

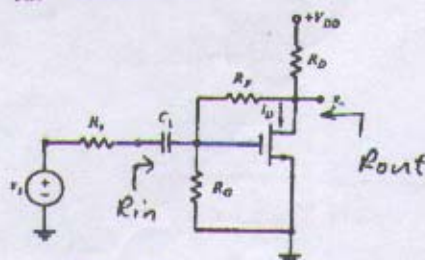
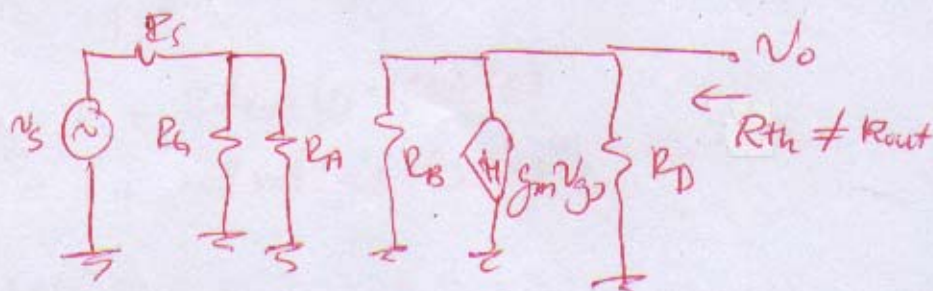


Figure 1



$$R_B \approx R_F \text{ because } (-g_m R_D) \gg 1$$

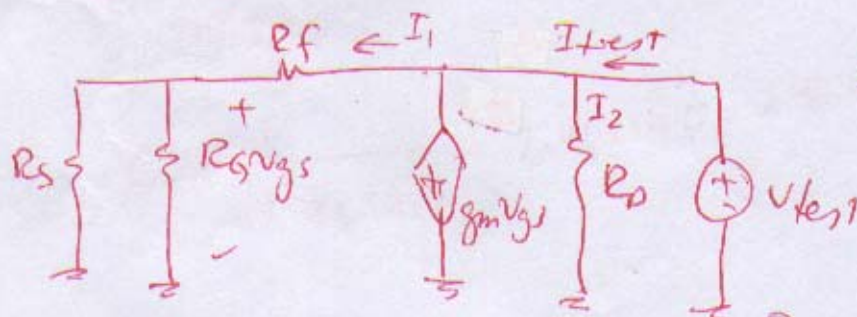
$$R_B \parallel R_D \approx R_D = 5 \text{ k}\Omega$$

$$R_A = \frac{R_F}{1 + 165} = 1.5 \text{ k}\Omega$$

$$R_{in} = R_G \parallel R_A \approx R_A = 1.5 \text{ k}\Omega$$

$$\frac{v_o}{v_s} = -165 \frac{R_{in}}{R_S + R_{in}} = -165 \frac{1.5}{5 + 1.5} = -38.22$$

R_{out} must be calculated from the ckt below:



$$R_{out} = \frac{v_{test}}{I_{test}}$$

$$v_{gs} = v_{test} \frac{R_G \parallel R_S}{R_F + R_G \parallel R_S} = \frac{1}{51} v_{test}$$

$$I_{test} = I_1 + I_2 + g_m v_{gs}$$

$$I_1 = \frac{v_{test}}{R_F + R_S \parallel R_G}, \quad I_2 = \frac{v_{test}}{R_D}$$

$$R_{out} = \frac{v_{test}}{\frac{v_{test}}{R_F + R_S \parallel R_G} + \frac{v_{test}}{R_D} + \frac{g_m v_{test}}{51}}$$

$$R_{out} = (R_F + R_S \parallel R_G) \parallel R_D \parallel \frac{51}{g_m} = 1.175 \text{ k}\Omega$$

(50 pts) For the BJT in Figure 2, $I_C = 1.5 \text{ mA}$, $h_{FE} = 350$, $f_T = 500 \text{ MHz}$, $C_\mu = 1.5 \text{ pF}$. Find the values of the capacitors C_1 , C_2 and C_E so that the low 3-dB cutoff frequency is no larger than 20 Hz.

$$C_1 = \underline{\hspace{2cm}}$$

$$C_2 = \underline{\hspace{2cm}}$$

$$C_E = \underline{\hspace{2cm}}$$

$$I_C = 1.5 \text{ mA}, \quad g_m = \frac{1.5}{0.025} = 60 \text{ mA/V}, \quad r_{\pi} = \frac{350}{60} = 5.8 \text{ k}\Omega$$

consider pole frequencies only

$$f_1 + f_2 + f_E \leq 20 \text{ Hz}$$

No unique solution!

C_E = dominant capacitor

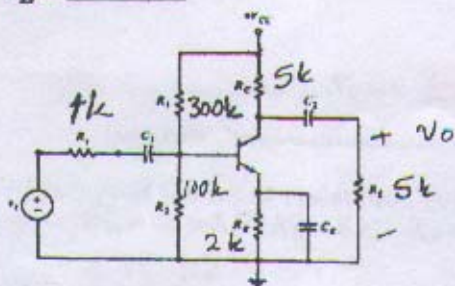


Figure 2

$$\text{let } f_E = 18 \text{ Hz}, \quad f_1 = f_2 = 1 \text{ Hz}$$

$$C_1 = \frac{1}{2\pi f_1 R_{th1}}, \quad R_{th1} = R_s + R_{1||2} || [r_{\pi} + (\beta_0 + 1) R_E]$$

$$= 1 + 100 || 300 || [5.8 + (351 \times 2)] \approx 68.7 \text{ k}\Omega$$

$$C_1 = \frac{1}{2\pi \times 1 \times 68700} = 2.3 \times 10^{-6} \text{ F}$$

$$C_2 = \frac{1}{2\pi f_2 R_{th2}}, \quad R_{th2} = R_c + R_L = 10 \text{ k}\Omega$$

$$= \frac{1}{2\pi \times 1 \times 10000} = 15.9 \times 10^{-6} \text{ F}$$

$$C_E = \frac{1}{2\pi f_E R_{thE}}, \quad R_{thE} = \frac{(1 || 100 || 300)^k + 5.8^k}{351} || 2k = 0.0192 \text{ k}\Omega$$

$$C_E = \frac{1}{2\pi \times 18 \times 19.2} = 2.96 \times 10^{-4} \text{ F} = 296 \times 10^{-6} \text{ F}$$