

Name :
Student ID :

Digital Systems II
Midterm II
2009-10 Spring, I/II Öğretim

27.04.2010
28.04.2010

90 minutes

SOLUTIONS

1.

2.

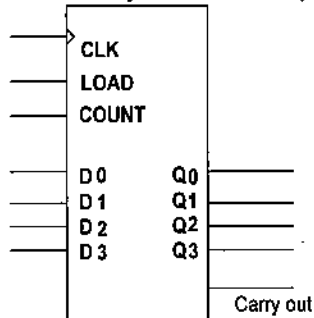
3.

4.

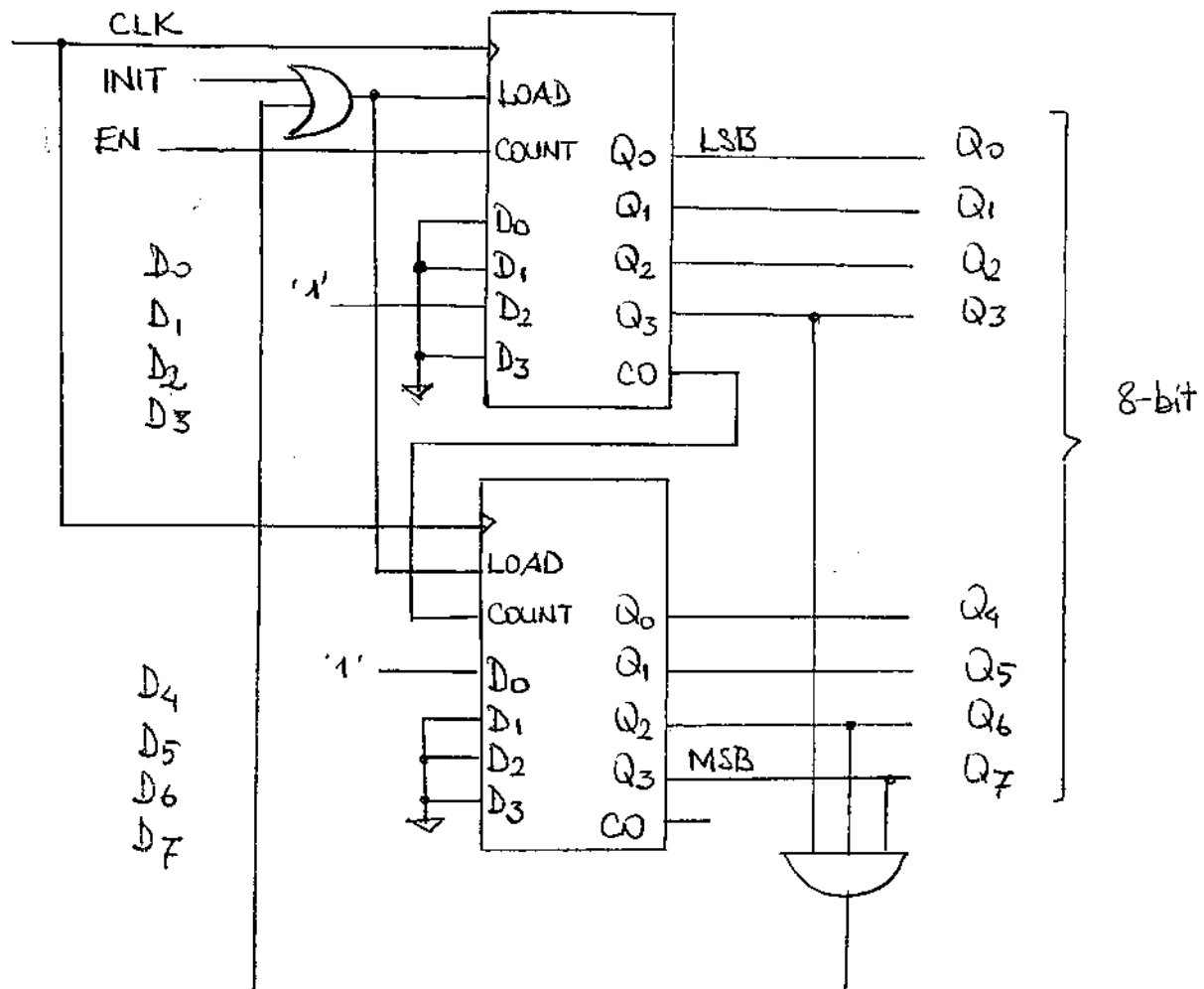
Counter Design

1. Using two 4-bit binary counters of the type shown below and logic gates, construct a binary counter that counts from decimal 20 through decimal 200. Add an additional input to the counter that initializes it synchronously to 20 when the signal INIT is 1. [20pts]

4-bit binary counter with parallel load



$$\begin{array}{cccccccc} Q_7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ (0 & 0 & 0 & 1 & 0 & 1 & 0 & 0)_2 = (20)_{10} \\ (1 & 1 & 0 & 0 & 1 & 0 & 0 & 0)_2 = (200)_{10} \end{array}$$



Register Transfer Structure: Dedicated Multiplexers

2. A system is to have the following set of register transfers:

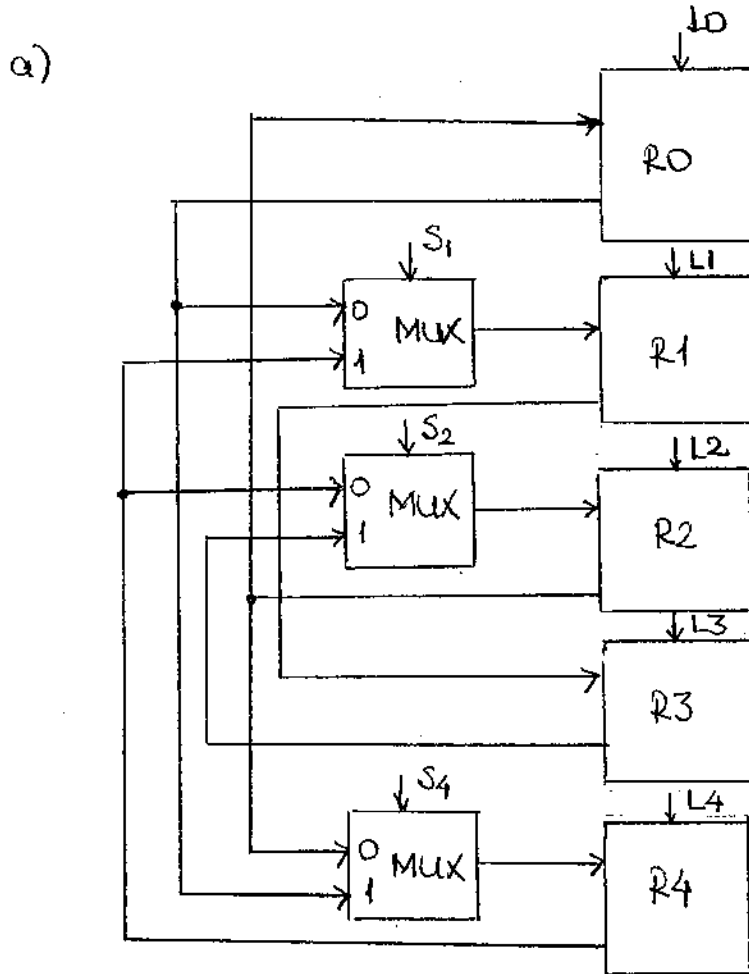
$$C_0 : R1 \leftarrow R0$$

$$C_1 : R3 \leftarrow R1, R1 \leftarrow R4, R4 \leftarrow R0$$

$$C_2 : R2 \leftarrow R3, R0 \leftarrow R2$$

$$C_3 : R2 \leftarrow R4, R4 \leftarrow R2$$

- a) Using registers and dedicated multiplexers, draw the logic diagram of the system hardware that implements these register transfers. [15pts]
 b) Design a simple combinational logic that generates the SELECT signals for the multiplexers and LOAD signals for the register using the control variables C_0, C_1, C_2 , and C_3 . [15pts]
 The control variables are mutually exclusive.



b)

Control Signals				Select			Load				
C_0	C_1	C_2	C_3	S_1	S_2	S_4	L_0	L_1	L_2	L_3	L_4
0	0	0	0	x	x	x	0	0	0	0	0
1	0	0	0	0	x	x	0	1	0	0	0
0	1	0	0	1	x	1	0	1	0	1	1
0	0	1	0	x	1	x	1	0	1	0	0
0	0	0	1	x	0	0	0	0	1	0	1

$$S_1 = S_4 = C_1$$

$$S_2 = C_2$$

$$L_0 = C_0$$

$$L_1 = C_0 + C_1$$

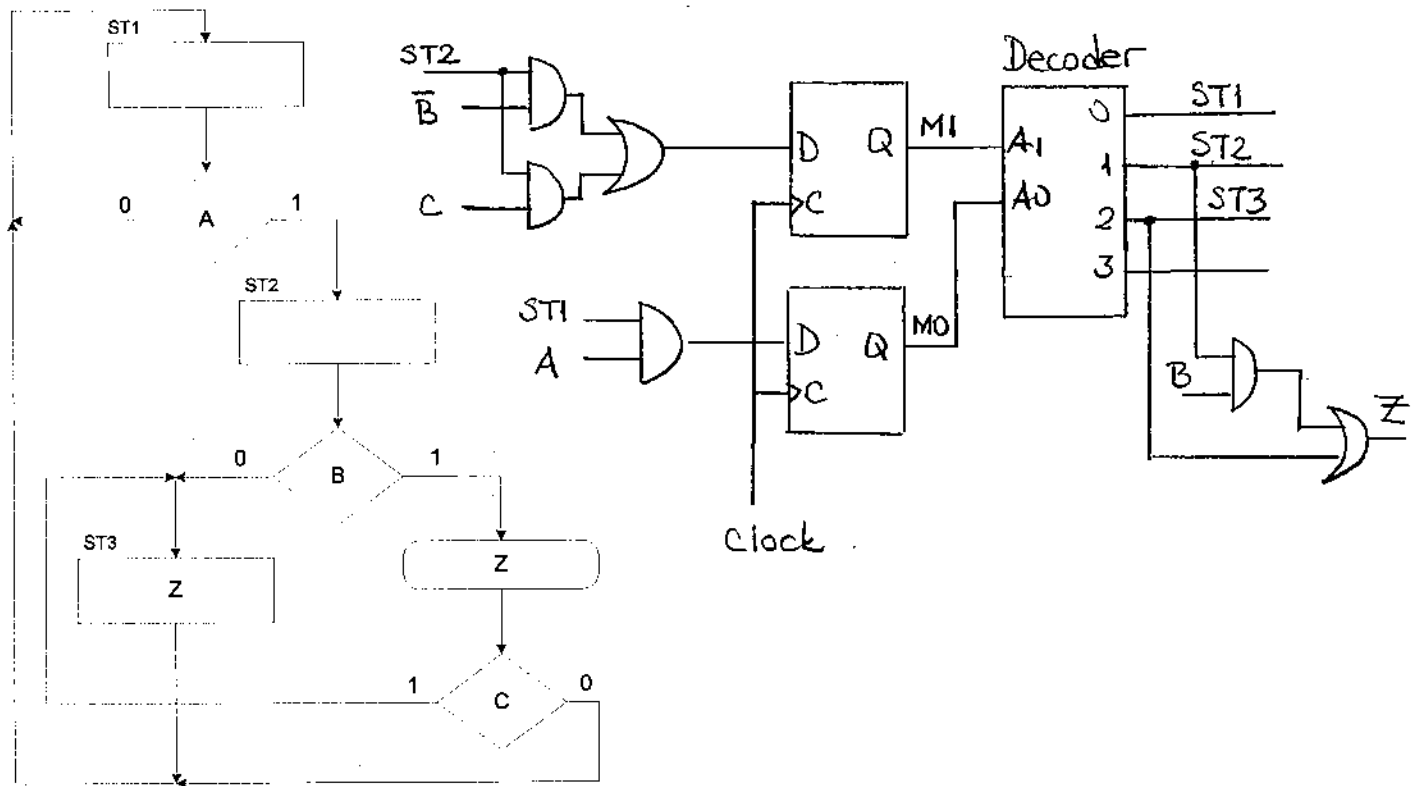
$$L_2 = C_2 + C_3$$

$$L_3 = C_1$$

$$L_4 = C_1 + C_3$$

ASM Chart

3. Implement the ASM chart using the sequence register and decoder. The controller has two inputs, A and B, C and one output Z. Draw the logic circuit. [30 pts]



State variables: M1, M0

State Table

	Present State		Inputs			Next State		Decoder Output		
	M1	M0	A	B	C	M1(t+1)	M0(t+1)	ST1	ST2	ST3
ST1	0	0	0	x	x	0	0	1		
	0	0	1	x	x	0	1	1		
ST2	0	1	x	0	x	1	0		1	
	0	1	x	1	0	0	0		1	
	0	1	x	1	1	1	0		1	
	0	1	x	1	1	1	0		1	
ST3	1	0	x	x	x	0	0			1

$$D_{M1} = M1(t+1) = ST2 \cdot \bar{B} + ST2 \cdot B \cdot C = ST2 \cdot \bar{B} + ST2 \cdot C$$

$$D_{M0} = M0(t+1) = ST1 \cdot A$$

Controller Design

4. Find the ASM chart for a traffic light controller. The controller has one input signal (T) and six Moore type outputs. The timing signal T defines the yellow light interval and also defines the changes of red and green lights. [20pts]

The controller operates as follows:

- If $T=0$, GN light goes on and RE light goes on.
- With $T=1$, YN light goes on and RE remains on.
- When $T=0$, both RN and GE lights go on.
- When $T=1$, RN remains on and YE goes on.
- The sequence repeats from the beginning.

GN	Green Light, North/South
YN	Yellow Light, North/South
RN	Red Light, North/South
GE	Green Light, East/West
YE	Yellow Light, East/West
RE	Red Light, East/West

